Solute relaxation on the solvatochromism of ortho-betaine dyes. A sequential Monte Carlo/quantum mechanics study

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Molecular relaxation in solution, estimated by thermodynamic perturbation theory, is shown to be important even for a qualitative description of the solvent effects on the solvatochromic shifts of flexible betaine dyes. It is shown that the most stable conformer of the ortho-betaine has a dihedral angle \( \varphi = 30^\circ \) in the gas phase and \( \varphi = 60^\circ \) in aqueous solution. This relaxation alone is responsible for about 30% of the overall blue shift observed in the \( \pi \rightarrow \pi^* \) transition of betaine in water. In addition, it was observed that the \( \pi \rightarrow \pi^* \) transitions are actually red shifted in the gas phase due to internal rotation. The total solvatochromism of about 6000 cm\(^{-1}\) estimated with a Monte Carlo/quantum mechanics sequential methodology is in reasonable agreement with the experimental shift of the absorption spectra in water and in toluene.

Introduction

Conjugated organic compounds that present large changes of the dipole moment upon electronic excitation are of great interest mainly due to the strong solvatochromic effects and their potential application to non-linear optics. These compounds have been used in the spectrophotometric determination of water in organic solvents and for establishing a quantitative solvent polarity scale to quantify the solvent effects on equilibrium constants and reaction rates. Since the early detailed solvatochromatic study performed by Reichardt and Dimroth, the pyridinium \( N \)-phenoxido betaine dyes (Fig. 1) have been extensively investigated for these purposes.

These dyes present a zwitterion-like structure in the electronic ground state, with positive and negative partial charges on the nitrogen and the oxygen atoms, respectively. This charge separation leads to very large ground-state dipole moments, with positive and negative partial charges on the nitrogen or to the carbon atoms of the pyridinium ring at the ortho position. The betainic character, that is, the charge separation, is usually lost in the excited states with a charge transfer character, and in this case, the dipole moment in the ground state \( (\mu_g) \) is much larger than that in the excited state \( (\mu_e) \).

Alkyl and aryl substituted pyridinium \( N \)-phenoxido betaines have been studied experimentally by several research groups. Paley et al. investigated the solvatochromic behavior of an ortho-betaine, 2,4-dimethyl-6-(2,4,6-triphenyl-N-pyridiniophenoxide) phenolate, for which they also obtained the crystallographic structure. The solvatochromic behavior of 2- and 4-pyridino phenoxides (Fig. 1a and 1b, respectively) has also been studied in a series of solvents. In addition, semi-empirical (AM1) and DFT (B3LYP/6-311G) methods have been employed with the self-consistent reaction-field (SCRF) approach to rationalize these experimental data.

Several other theoretical treatments have been used to describe these betainic systems and their solvatochromatic behavior, such as the single configuration interaction (CIS) study of the para-pyridiniophenoxide (Fig. 1b), where gas phase DFT molecular structures have been used to take into account the effects of the internal rotation on the calculated spectra in solution. In fact, this molecular relaxation (internal rotation) appears to be quite important to understand the solvatochromic shifts. Also, Monte Carlo simulations of the \( E_r(30) \) Reichardt betaine dye in twelve solvents have been performed aiming at understanding the molecular basis of the solvent polarity scale. In that study, \( ab \) initio (HF/6-31G\(^*\)) and
semi-empirical (AM) and INDO/S) methods have been used to determine the molecular structure and the charge distribution on the S₀ and S₁ states, in the gas phase. The solvent effects were derived from the electrostatic interactions between the effective charge distributions of the solvent molecules and the charge shift brought about by the S₀ → S₁ transition. The dynamics of the E(T grown Betain dye excited state has also been studied, in acetonitrile, using a hybrid classical/quantum molecular dynamics method. The π electrons of the solute have been treated quantum mechanically (PPP Hamiltonian), including the solvent influence on electronic structure, while the remaining interactions are treated via empirical potentials. As a result, the internal rotations were taken into account but no attempt was made to explain the solvatochromic behavior of this system.

The main concern of the present work is then the calculation of the solvatochromism of one betaine taking into account the internal rotation between the phenoxide and the pyridinium rings. To accomplish this theoretical study we have chosen the ortho-betaine isomer (Fig. 1a) since it contains the basic donor–acceptor moieties of more complex betaines, such as the E(T grown Betain dye. Also, the ortho-betaine is small enough to be treated by ab initio methods and the effects of bulky groups are absent, so that the importance of the internal rotation or molecular relaxation in solution can be unambiguously ascertained. In addition, there is significant spectroscopic information about the solvatochromic behavior of this ortho-betaine in several solvents. After choosing the appropriate betaine, a sequential hybrid quantum mechanical/Monte Carlo methodology has been selected to study the solvatochromism and the effects of the molecular relaxation (internal rotation) in solution. More specifically, the Monte Carlo method has been used to yield statistically significant configurations of the solute–solvent system that were then treated by quantum chemical methods to obtain spectroscopic information. The combination of these methods in a sequential fashion should provide reliable theoretical results for a quantification of the effects of the internal rotation in the total solvent effects. As the solvent, we have chosen water as it gives the largest blue shift in the absorption spectrum where also the influence of hydrogen bonds can be studied.

Theoretical and computational procedures

The internal rotation or molecular relaxation is described by the dihedral angle between the phenoxide and the pyridinium rings, labeled φ, as shown in Fig. 1a. The ab initio MP2/6-31G method implemented in the Gaussian98 program has been used to calculate the electronic and molecular structures and the electrostatic potential (ESP) fitted atomic charges of the ortho-betaine at thirteen points on the reaction coordinate from 0° to 90° with a 7.5° step. Those 13 molecular structures were later used in the molecular simulations with rigid geometries and its respective atomic charges. In Fig. 2, the calculated charges of the oxygen and the nitrogen atoms and the dipole moment of the ortho-betaine are shown.

The interaction between the solute (ortho-betaine) and the solvent (water) is represented by a Lennard-Jones plus a Coulomb pair-wise potential. The SPC/2 parameters were used for the water molecules and the ESP fitted charges for the Coulombic part of the solute potential (see Fig. 2). The Lennard–Jones parameters (ε, σ) for the ortho-betaine were obtained from the phenol and the pyridine molecules. The standard geometric combination rules were used to generate the pairwise parameters. After defining the interaction potential, the Monte Carlo (MC) simulations were performed using standard procedures for the Metropolis sampling technique in the canonical (NVT) ensemble, with periodic boundary conditions, image method and long range correction for the energy beyond the cut-off radius. The Lennard-Jones potential contribution is estimated assuming a uniform distribution G(ε) = 1 after the cutoff radius and the electrostatic potential contribution is estimated with the reaction field method of the dipolar interaction. The cut-off radius was considered as half-size of the cubic box length. The system was formed by one of the 13 molecular structures of the ortho-betaine surrounded by N = 900 water molecules. The experimental value for water density (ρ = 0.9986 g cm⁻³) at 25 °C was used to determine the size of the cubic box (L = 3.011 nm). The initial configurations were generated randomly and a new MC configuration was generated after N MC steps, i.e. after N molecules have been randomly selected and attempted to move.

The MC simulations were performed with DICE and involved a thermalization stage of 9 × 10⁶ MC steps followed by an average stage of 72 × 10⁶ MC steps. In this averaging stage several thermodynamic and structural properties are calculated. Of special interest are the radial distribution functions and the variation of the Helmholtz energy due to the relative conformational stabilization of the ortho-betaine in aqueous solution. The relative Helmholtz energy, ΔA(φf - φi), calculation is implemented in the MC simulation using the thermodynamic perturbation theory (TPT), and was evaluated with a series of 6 separate simulations with the ortho-betaine in the rigid geometry but varying the torsion angle. We used the double-wide sampling, i.e., 6 simulations yielded 12 incremental free energy changes by perturbing the torsion angle φf to both sides: the smaller φf = φi - 7.5° and the larger φf = φi + 7.5°, in each simulation. Consistent results have been obtained with TPT in various chemical and biochemical studies.

Instead of performing a quantum mechanical calculation on every configuration generated by each simulation, we used the auto-correlation function or statistical efficiency, to select the statistically relevant configurations. In doing so, the subsequent quantum mechanical calculations were performed only on some uncorrelated structures. As in previous works, we fitted the auto-correlation function of the energy to an exponentially decaying function and evaluated the correlation step. For the ortho-betaine in water, we obtained that configurations separated by an interval of 1.18 × 10⁶ MC steps have less than 3% of statistical correlation. This assures that the configurations used in the quantum mechanical calculations are statistically uncorrelated and yield the same average values as the entire set of configurations. Therefore, for each
simulation, we selected configurations separated by $1.18 \times 10^6$ successive configurations, generating a total of 61 statistically uncorrelated configurations, in which the quantum mechanical calculations were evaluated and averaged out.

The excitation energies were calculated using the Florida INDO program within the INDO/CIS model for the supermolecules generated by the MC simulation. The QM calculations were then performed for the supermolecular cluster composed of one ortho-betaine and all water molecules within a particular solvation shell. Each water molecule includes 8 valence electrons, and the Hartree–Fock wave function is anti-symmetric with respect to the entire solute–solvent system. CIS calculations were performed to obtain the excitation energies for all statistical uncorrelated configurations. The solvatochromic shift is obtained as the average over the 61 energies for all statistical uncorrelated configurations. The solvent effects on the conformation of the ortho-betaine have been calculated with the free-energy perturbation theory. These effects can be visualized by comparing the gas phase internal rotation energy (MP2/6-31G) and the Helmholtz energy internal rotation (TPT-MC) as shown in Fig. 3. There are significant qualitative as well as quantitative differences between the internal rotation in the gas phase and in water. The most stable conformer is shifted from approximately 30° in the gas phase to near 60° in water. This shift is due to the hydrogen bonding between the oxygen atom of the ortho-betaine and the hydrogen atom of water, as shown in Fig. 4a. The RDF between the oxygen atom of the ortho-betaine and the hydrogen atom of water is shown in Fig. 4b.

The radial distribution function, RDF, for the most stable conformer in solution ($\varphi = 60°$), is shown in Fig. 4. Fig. 4a shows the RDF between the oxygen atom of the ortho-betaine and the hydrogen atoms of the water. Fig. 4b shows the RDF between the oxygen atom of the ortho-betaine and the oxygen atom of the water. The RDF shows the closest atoms between the solute and solvent molecules. This is a nearest-neighbor RDF that is more appropriate in defining the solvation shell for betaine. It is of interest to analyze separately the contribution of the hydrogen bonds. The criteria utilized to classify a hydrogen bond was composed of a geometrical (radial distance $R_0 \leq 3.35 \text{ Å}$ and angular $\phi < 30.0°$) and an energetic ($E_{\text{HB}} \geq 3.6 \text{ kcal mol}^{-1}$) contribution. The adequacy of this procedure has been discussed elsewhere. We find that in 8.2% of the configurations the phenoxyde oxygen makes one hydrogen bond with water molecules, in 54.1% of the configurations it makes two hydrogen bonds and in 37.7% it makes three hydrogen bonds. In total, we find that there is an average of 2.3 hydrogen bonds for the phenoxyde oxygen atom (proton acceptor). This is termed as the HB shell. Fig. 4c shows additional hydration shells for the ortho-betaine at this conformation. As it can be seen there is a clear nearest-neighbor solvation shell that starts at 1.5 Å and ends at 4.0 Å, that gives a total of 30 water molecules. After this, only a broad feature is observed, but it is still possible to note some structure that ends at around 7.45 Å, that gives a total of 50 water molecules. To have a larger cluster for the quantum mechanical calculations we use the hydration shell distances of 9.65 Å yielding 120 water molecules.
around the ortho-betaine and of 10.40 Å yielding 150 water molecules. Table 1 specifies the hydration shells that are used in the quantum mechanical calculations of the electronic spectrum. Note that in the HB shell, in the total of 61 configurations used in the quantum calculations, 5 have only one water molecule bonded in the ortho-betaine, 33 have two water molecules and 23 have three, giving a total of 72, 82 and 88 valence electrons, respectively.

The selected configurations have been submitted to quantum chemical calculation with the INDO/CIS model to obtain the solvent effects in the transition energies. Quantum mechanical calculations are made with several cluster sizes to analyze the influence of the outer solvation shells in the solvatochromic shift. The bulk result can then be obtained extrapolating the calculating transition energy shifts for different solvation distances, as shown in Fig. 5. The results for the individual contributions of each hydration shell, including the bulk limit, to the solvatochromism of the ortho-betaine are summarized in Table 2. We first analyze the influence of the torsion angle on the gas phase spectrum. Changing the angle from 30° to 60° yields significant shifts. The first π → π* transition is red shifted by nearly 2000 cm⁻¹, whereas the first n → π* transition suffers a blue shift of 1600 cm⁻¹. In Fig. 6, the filled circles show the effect in the first n → π* transition due to the changing in the torsion angle relatively to the transition value in the 30°. As can be seen for torsion angles smaller than 30° the transition energy is red shifted, reaching ~3167 cm⁻¹ in the planar conformation (i.e. φ = 0°). Whereas for torsion angles larger than 30° the transition is blue shifted, reaching 1602 and 1607 cm⁻¹ for conformations with φ = 50° and 60°. This curve shows that conformational changes in the ortho-betaine can induce a shift of around 4800 cm⁻¹ in the first n → π* transition.

The influence of the solvent is given in the lower part of Table 2. Adding the HB shell yields pronounced shifts for all absorption bands considered here. However, these are still very small compared to the total shifts. The n → π* transition suffers a blue shift of 3136 cm⁻¹ due to the HB shell, which can be separated into 1529 cm⁻¹ due to the electronic contribution and 1607 cm⁻¹ due to the solute relaxation. Table 2 also gives the separate contribution of the hydration shell to the total calculated solvatochromic shifts.

The final calculated solvatochromic value of 6060 ± 89 cm⁻¹ for the n → π* transition is in reasonable agreement with the observed value of 7552 cm⁻¹, obtained as the shift of the maximum in the absorption spectra of the ortho-betaine in water and toluene.¹⁰ The difference is probably due to inherent deficiencies of the INDO/CIS method as well as due to the effects of other conformations near 60°, since the Heliomolz energy is somewhat flat around the minimum. The difference is also due to the comparison between the gas phase with the solvatochromic shifts. It can be seen that changing the dihedral angle from 30° to 60° causes, in the gas phase, a red shift of all π → π* transitions, which can be as large as 1986 cm⁻¹, and a blue shift of 1607 cm⁻¹ for the n → π* transition. These results show the importance of the molecular relaxation for the absorption spectrum. Regarding the solvent effects, Table 2 presents the solvatochromism of the most stable conformer in water (φ = 60°) with respect to the most stable conformer in the gas phase (φ = 0°).

It is worthwhile noticing that the solvent causes a blue shift for the π → π* transition. In fact, these data contain both the molecular relaxation and the solvent effects. Assuming that these effects are additive, the shift due to only the solvent effects can be estimated by subtracting off the molecular relaxation shift obtained from the gas phase calculation. This procedure yields the “net solvent effects” on the solvatochromism, which are listed in the last row of Table 2. In Fig. 6, the open circles show the effect of the 120 water molecules in the first n → π* transition relatively to the transition value of the isolated ortho-betaine in the 30° conformation. The net solvent effect is the difference between the filled and the open circles for each torsion angle. The smallest effects, around 1000 cm⁻¹, can be seen for torsion angles smaller than 40° and the largest effects, around 4500 cm⁻¹, can be seen for torsion angles larger than 70°. Depending on the conformation of the ortho-betaine the net solvent effect can vary from 934 to 4636 cm⁻¹ and therefore the net solvent effects can be larger or smaller than the molecular relaxation effects. Thus those two effects, solvent and geometry relaxation, are both very important for a qualitative and quantitative description of the solvatochromism. The solute relaxation is also important for understanding the solvent polarity scale associated with the solvatochromic shifts of the E(r(30)) Reichardt dye.¹⁴,¹⁵,¹⁵

![Fig. 5 Extrapolation of the calculated n → π* transition energy to the bulk limit. HB, first, second and others hydration shells are shown.](image)

Table 2 Transition energies (in cm⁻¹) and solvatochromic shift (in cm⁻¹) for the ortho-betaine in the gas phase (φ = 30°) and aqueous solution (φ = 60°)

<table>
<thead>
<tr>
<th>Gas phase</th>
<th>π → π*</th>
<th>n → π*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Transition energy (φ₉₀)</td>
<td>15612</td>
<td>22798</td>
</tr>
<tr>
<td>Transition energy (φ₆₀)</td>
<td>13626</td>
<td>24405</td>
</tr>
<tr>
<td>ΔE (φ₆₀ - φ₉₀)</td>
<td>-1986</td>
<td>1607</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>HB</th>
<th>First</th>
<th>Second</th>
<th>Others</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of water molecules in the shell</td>
<td>~2.3</td>
<td>30</td>
<td>50</td>
</tr>
<tr>
<td>Number of valence electrons for each shell</td>
<td>~82</td>
<td>304</td>
<td>464</td>
</tr>
<tr>
<td>Average distance hydration shell-solute/A</td>
<td>3.35</td>
<td>4.00</td>
<td>7.45</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>δE = transition energy at 60° – transition energy at 30°</th>
</tr>
</thead>
<tbody>
<tr>
<td>δE[(φ₆₀ + HB) - φ₉₀]</td>
</tr>
<tr>
<td>δE[(φ₆₀ + 30H₂O) - φ₉₀]</td>
</tr>
<tr>
<td>δE[(φ₆₀ + 50H₂O) - φ₉₀]</td>
</tr>
<tr>
<td>δE[(φ₆₀ + 120H₂O) - φ₉₀]</td>
</tr>
<tr>
<td>δE[(φ₆₀ + 150H₂O) - φ₉₀]</td>
</tr>
<tr>
<td>δE[(φ₆₀ bulk limit) - φ₉₀]</td>
</tr>
<tr>
<td>Net solvent effects</td>
</tr>
</tbody>
</table>

* The error is associated with the standard deviation of the 61 configurations used. b The estimate value and the error is related to the linear regression fitting as can be seen in Fig. 5.
In the case of the most stable conformer in water (\( \varphi = 60^\circ \)) shown in Table 2, the internal rotation relaxation amounts to nearly 30% of the total computed shift. It should also be emphasized that the simulation of the solvent by only including hydrogen bonded molecules is inadequate even for a qualitative description. Indeed the blue shift of the \( \pi \rightarrow \pi^* \) transitions is not obtained if only the HB shell is considered. In fact, cluster calculations need to consider at least 50 solvent molecules to yield a qualitative result, and nearly 150 molecules for a reasonable quantitative description. The necessity of including outer hydration shells extending far beyond the solute is likely to be a consequence of the large dipole moment of betaines.

Conclusions

It has been shown that the molecular relaxation due to the solvent effects on the conformation is quite important for a proper description of the solvatochromism of the flexible ortho-betaine. In fact, the molecular relaxation has an opposite effect on the solvatochromic shift for the \( \pi \rightarrow \pi^* \) transitions when compared to the net solvent effects. These approximately separated contributions to the solvatochromism allowed the quantification of the molecular relaxation effects, which are significant for even a qualitative description.

Acknowledgements

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References